Optical waveguiding by necklace and azimuthon beams in nonlinear media

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Nonlinear necklace and azimuthon beams were experimentally generated in a self-focusing bulk photorefractive nonlinear medium (crystal SBN:60) using a frequency-doubled Nd:YVO₄ laser at 532 nm. The parallel optical waveguides induced by such a beam were probed by near-infrared signal beams emitted by a Ti:Sapphire laser. The quality and time stability of the guided sub-beams at the exit of the crystal were investigated. In view of the waveguides’ ordering along a ring, the best matching probe beams were found to be singly or doubly charged optical vortex bright rings. The results indicate the feasibility of parallel all-optical guiding of optical signals at wavelengths, for which the nonlinear medium is not photosensitive.

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1. INTRODUCTION

Spatial optical solitons [1,2]—stationary self-trapped localized beams in third-order nonlinear media—belong to the most intensively studied nonlinear objects. As early as in the first analysis, the authors formulated the concept of all-optical wave-guiding [1], which stimulated intensive research: because the beam, once trapped, establishes a waveguide of appropriate characteristics for its own conduction, weak waves can be conducted [1]. As is known, optical solitons in media with an instantaneous isotropic self-focusing nonlinearity are unstable due to the critical collapse at high powers [3–6]. In a local saturable self-focusing nonlinear medium (NLM), however, one observes robust self-trapping of optical vortex beams over several Rayleigh diffraction lengths [7].

In the context of bright optical beams, the soliton cluster has been introduced in [8,9] as a multi-soliton bound state in a homogeneous bulk optical NLM. Its rich transverse dynamics [10] can be intuitively understood recalling that, depending on their relative soliton phase \( \delta \theta \), in general, two spatial solitons attract for \( \delta \theta = 0 \) or repel each other for \( \delta \theta = \pi \) [11]. Similarly, considering \( \delta \theta \) as the magnitude of the phase jump between two solitons of the cluster, when \( 0 < \delta \theta < \pi / 2 \), the interaction between solitons is attractive, whereas for \( \pi / 2 < \delta \theta < \pi \) it is a repulsive one. In the particular case \( \delta \theta = \pi \), as shown in Fig. 1(a), the cluster expands without rotation as a necklace-type beam [8,12]. The intensity of the necklace beam is periodically modulated azimuthally and the adjacent bright sub-beams on the ring differ in phase by \( \pi \) [Fig. 1(a)]. The necklace beam is predicted to be stable in nonlinear media for \( (2 + 1) \) spatial dimensions when the azimuthal period of the ring (the sub-beam-to-sub-beam distance) is much smaller than the ring radius (i.e., the ring curvature vanishes). The necklace-ring beams expand slowly but fully preserve their structure [8]. More precisely, the analyses have shown [13] that the incoherent interaction between the components of a vector ring-like beam allows one to compensate for the coherent repulsion of the sub-beams, so that stationary self-trapped necklace-ring vector solitons can be formed. A comprehensive overview of the early results on necklace beams and ring-like soliton clusters can be found in [14]. The concept of multipole vector spatial solitons formed by the interaction of co-propagating, mutually incoherent optical beams in a saturable bulk NLM has been presented in detail in [15].

The azimuthons were introduced for the first time in [16] as spatially localized self-trapped ring-like singular optical beams [Fig. 1(b)] in NLM. They appear due to a continuous azimuthal deformation of vortex solitons and, in contrast with the necklace beam, carry a net angular momentum. As opposed to the linear vortex phase \( \psi = m \theta \) [see Fig. 1(c)], where \( m \) is the vortex topological charge (TC) and \( \theta \) is the polar angle, the phase of the azimuthon is a staircase-like nonlinear function of \( \varphi [16] \), as shown in Fig. 1(b). The azimuthon family includes clusters with negative, positive, and zero angular velocity, defined by the phase inclination \( \alpha \), as indicated in Fig. 1(b).
The rotation can be suppressed by a uniform energy flow along the ring; the azimuthon then remains stationary [16].

The first experimental generation of optical azimuthons utilized picosecond laser pulses in a Kerr nonlinear medium, demonstrating azimuthons of order 3 and 13, having a trivial phase profile [17]. Later, [18] reported on the observation of optical azimuthons with three and four lobes and a complex phase profile, generated by phase imprinting in hot Rb vapors. It was shown that the presence of azimuthal intensity and phase modulation leads to spatial rotation of the azimuthon in the self-focusing NLM [18], where the nonlinear interaction of azimuthon lobes slows down and even inverts the direction of rotation. Furthermore, [19] showed that even a Bose–Einstein condensate trapped by an annular potential induced by a Laguerre–Gaussian pump supports azimuthons. In this physical system, azimuthons can form spontaneously due to the presence of thermal noise. Finally, the formation of self-trapped dipole azimuthons has been demonstrated in nematic liquid crystals [20], as being due to these crystals’ re-orientational nonlinearity.

Despite such general interest in optical necklace beams and azimuthons in particular, their guiding properties have not been the subject of thorough studies. To the best of our knowledge, we present here, for the first time to the best of our knowledge, a study on the waveguiding properties of optical necklace and azimuthon beams in a photorefractive nonlinear medium at 532 nm. We show that, as a consequence of their self-focusing, such beams can guide other strong beams at non-photosensitive wavelengths.

2. EXPERIMENTAL SETUP

Four-lobe necklace beams and azimuthon beams were generated in the following way: we let the input Gaussian beam diffract in the first diffraction order from a computer-generated hologram (CGH) of a quasi-2D dark beam [see Fig. 2(a)] or in second/fifth diffraction order of the CGHs of optical vortices (OVs), as shown in Figs. 2(b) and 2(c), respectively. Thus, in the second diffraction order of the CGH, as shown in Fig. 2(b), we obtained a linear azimuthon beam with five bright lobes. Alternatively, in the fifth diffraction order of the CGH in Fig. 2(c), we obtained a linear azimuthon with 10 lobes.

From the CGH of the quasi-2D dark beam [Fig. 2(a)], we produced four bright subpeaks of a necklace beam. Self-focusing was initiated in a photorefractive SBN:60 crystal. The CGHs of the singular beams used were of a binary type, produced photolithographically with a grating period of 20 μm [Figs. 2(a) and 2(b)] and 30 μm [Fig. 2(c)]. Due to their binary nature and the necessity to have curved reflecting stripes consisting of two pixels of 5 μm width for the 20 μm grating and 3 pixels of 5 μm width for the 30 μm grating, in some areas 1 pixel disappears on one side of the stripe appearing farther on its opposite side. As a result, on the holograms of the vortices we observed a specific azimuthal modulation of the grating transmission/reflection [see the microscope photographs shown in Figs. 2(b) and 2(c)]. This modulation, however, results in a phase modulation of the diffracted beams and is multiplied by the diffraction order. In this way, bright azimuthon sub-beams surrounding the OV core were reproducibly experimentally generated, well separated by dark radial stripes. In the case of a necklace structure with four peaks, the hologram used [see Fig. 2(a)] splits the input Gaussian beam in four sub-peaks due to the encoded crossed 1D (diagonal) phase jumps by π. The experimental setup (Fig. 3) involved a green pump beam from a frequency-doubled continuous-wave Nd:YVO4 laser carrying the desired phase singularities and the surrounding ring-like ordered bright sub-beams, which further self-focus in the SBN crystal. The probe beam used for testing the properties of the induced waveguides and their time stability was a near-infrared continuous-wave beam emitted from a Ti:Sapphire laser. For diagnostic purposes, the beam of the green laser was split by a beam splitter (BS) and, later, the object and the reference beams were recombined by a second BS to interfere at the CCD camera chip. Behind the CGHs, the desired diffraction order beam was selected by an iris diaphragm D and focused by a lens FL on the front facet of a 6 mm long SBN:60 photorefractive crystal of a cross-section 6 mm × 10 mm. The laser beam polarization was parallel to the crystalline c axis; thus the beam experienced strong photorefractive nonlinearity due to the high electro-optic coefficient r33 in the SBN. The crystal was biased by an electric field E0 ranging from 600 V/cm to 700 V/cm. The front or back facet of the crystal was imaged by a lens IL onto a charge-coupled device (CCD) camera, both moving on translation stages. Power density distributions of the resulting optical beams and the respective interference patterns were recorded by the same CCD camera by

Fig. 2. Computer-generated holograms of (a) a quasi-2D dark beam, of (b) an OV with TC = 1 and grating period of 20 μm, and, again, of (c) a singly charged OV with a grating period of 30 μm. The areas of azimuthal modulations are depicted by rotated arrows to remind the reader of the OV helical phase profiles.

Fig. 1. Intensity (top) and phase (bottom) structure of different types of spatial soliton beams: (a) four-lobe necklace type beams; (b) five-lobe azimuthon beam. The general phase shape can feature a non-zero phase-tilt across each lobe. (c) Vortex-type beam.
one generating an optical vortex beam (OV) with a single or double charge. For this purpose, in the probe arm of the setup, we placed another CGH encoded with an OV of the desired TC. The first diffraction order beam was selected by a diaphragm and then matched to the previously induced waveguides in the SBN crystal.

3. RESULTS AND DISCUSSION

Regardless of the number of bright lobes in the necklace and in the azimuthon structure, all measurements presented here refer to a mean power of the green laser of 110 μW measured before the focusing lens. The crystal illumination time was 5 min, and the electric field applied on the SBN crystal was 650 V/cm.

In Table 1 we show the measured values of the total (peak-to-peak) width of the structures on the front facet of the SBN crystal, on its exit facet after linear diffraction, and the size of these beams on the exit facet after the nonlinear process of self-focusing has been initiated. Data also are shown for the sizes of the individual lower (or lower left) single peak for each of these bright structures. In these notations, \( x \) is the horizontal Cartesian coordinate system axis, \( y \) is the vertical one. These measured beam sizes (see Table 1) are strong evidence for the clear experimental discrimination between linear propagation (2D diffraction) and the initial stage of nonlinear self-focusing. Bearing this in mind, we can conclude that, in the regime used, the nonlinearity clearly dominates over the diffraction, and the induction of the parallel waveguides in the crystal is a result of a nonlinear interaction. We also measured the angular spreading of the generated azimuthons. The data show that the linear divergence of the azimuthon with five lobes is 16 mrad, whereas for the azimuthon with 10 lobes it increases to 24 mrad. In the nonlinear case, the divergence of the five-lobe structure increases from 16 to 18 mrad still remaining smaller as compared with this for the 10-lobe structure—20 mrad. These data are accurate to within ±1 mrad. Our estimations also indicated that the necklace beam experiences linear and nonlinear divergences of 15 and 17 mrad, respectively, accurate to within ±0.7 mrad. In Fig. 4 we present gray-scale images of the recorded power density distributions of the input necklace (upper left-hand frame) and the input azimuthons (upper middle and right-hand frames) and the respective data on the exit facet of the crystal after linear diffraction (middle row) and after the nonlinear process of self-focusing (lower row). All recorded frames are blocking/unblocking the reference laser beam, while keeping the camera position unchanged. Special attention was paid to the CGHs alignment in order to place the dark singular beams well centered with respect to the illuminating beam. The power of the background beam was adjusted so as to initiate weak beam self-focusing only. We refrained from further increasing the background beam power to avoid filamentation in the crystal. In this way we created optically induced waveguides in the photorefractive NLM.

The probe beam in this setup was the output beam of a Ti: Sapphire continuous-wave laser operated at a wavelength of 808 nm. We first used the direct-output Gaussian beam as a probe beam, but this resulted in a dominating central peak, and the induced waveguiding was not well seen. In order to obtain better spatial matching of the probe wave with the necklace and azimuthon guiding structures in the bulk SBN crystal, we changed the beam profile to a Laguerre-Gaussian

![Fig. 3. Experimental setup. Nd:YVO4, continuous-wave frequency-doubled laser emitting at a wavelength λ = 532 nm; Ti:Al2O3, titanium-sapphire continuous-wave laser generating the probe beam at λ = 808 nm. BS, beam splitters; DM, dichroic mirror; CGH, binary computer-generated holograms; D, diaphragms; FL, focusing lens (f = 3.5 cm); M, flat silver mirrors; SBN, photorefractive crystal; IL and CCD, imaging lens and charge-coupled device (CCD) camera, both moving on a translation stages, imaging the front or the exit facet of the SBN crystal.](image-url)

### Table 1. Comparison between the Width of the Necklace Beam with Four Sub-beams and of the Vortex Azimuthon Beams with 5 and 10 Lobes on the Front Facet of the Crystal, on the Exit Facet in the Linear Regime of Propagation and, on the Exit Facet, but After the Nonlinear Process of Self-focusing has been Initiated

<table>
<thead>
<tr>
<th>Number of Peaks</th>
<th>On the Front Facet of the Crystal</th>
<th>On the Back Facet After Linear Diffraction</th>
<th>On the Back Facet After Self-Focusing</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Single Peak Size [μm]</td>
<td>Width [μm]</td>
<td>x_{in}</td>
</tr>
<tr>
<td>4</td>
<td>553 164 200</td>
<td>729 211 300</td>
<td>753 100 170</td>
</tr>
<tr>
<td>5</td>
<td>544 199 204</td>
<td>745 254 260</td>
<td>762 160 170</td>
</tr>
<tr>
<td>10</td>
<td>771 124 191</td>
<td>1064 160 240</td>
<td>1013 80 160</td>
</tr>
</tbody>
</table>

*The sizes of a single lower/lower left peak from these structures in the same three cases (see Fig. 4) are shown, too.*
directly comparable in size because the CCD camera positions were reproducible.

In Fig. 5 we show experimental evidence of the nonlinear phase structure of the generated azimuthons in the particular case of a 10-lobe structure. In the nonlinear regime shown in the right-hand column in this figure, the sub-beam's peak intensity is approximately three times higher as compared with the linear case. At the maximum 3.5 times increase of the peak lobe intensity in this measurement (not shown), the results were qualitatively similar: Even at a nonlinearly accelerated broadening of the radial dark beams, the interference half-rings between the azimuthon lobes, especially the inner 3–4 interference arcs, remain clearly offset in the radial direction (see the arrows in Fig. 5). Hence, the typical azimuthal staircase-like phase structure of the azimuthons [see Fig. 1(b)] survives the initial stage of its weak self-focusing.

With the setup shown in Fig. 3, we studied every single case separately. In addition to the weak self-focusing of the bright sub-beams and the inscription of waveguides, we also examined the guiding of a probe beam in these parallel guiding structures.

The first experimental set of data shown in Fig. 6 concerns the case of a bright azimuthon with 10 lobes and a central optical vortex with a TC = 1. This azimuthon was created by a CGH [Fig. 2(c)] of an OV with a TC = 1 diffracted from the CGH in the fifth diffraction order. The highest efficiency in the first diffraction order of the binary CGHs we used was typically close to the 10% limit predicted [21] and decreased drastically as the diffraction order was increased. In view of the relatively high laser power required in front of the CGH, this was the most difficult case to study experimentally in this work. (Of course, reflective liquid-crystal phase modulators can improve this situation.) We managed to nonlinearly achieve a relative increase of the beam's intensity from about four times for the least self-focused lobe up to six times for the most strongly focused lobe. The 808 nm probe beam was an optical vortex ring carrying an OV with a TC = 2. The input (a) and the self-focused output azimuthon structure (b) are shown in the left column in Fig. 6, respectively, whereas the exit probe beam (c) without and (d) with inscribed waveguides is shown in the right column of the same figure.

The applied electric field was parallel to the crystalline c axis; thus, the nonlinearity slightly dominated along the horizontal (x) direction across the azimuthon beam. This can be seen in Fig. 6(b), upper row, and (somewhat better) in the 3D view of the same distribution. As seen, the strongest self-focused bright lobes are located along the horizontal (x) axis, while along the perpendicular (y) axis the process is relatively weaker. In the two right-hand columns with experimental frames in Fig. 6, one can see the exit probe beam profile at no inscribed waveguiding structure (c) and its reshaping after passing through the optically induced ring-like ordered waveguides.
The continuous-wave probe beam emitted by the Ti:Al₂O₃ laser (λ = 808 nm) passed through a CGH of an OV with a TC = 2. The singular probe beam created in this way was used in a cw mode, although generation of OVs in the broad-bandwidth fields of femtosecond mode-locked lasers is a solved problem [22–25]. As seen in Fig. 6(d), all inscribed waveguides are well illuminated by this probe beam, and the guided peaks appear clearly visible and well-formed. The obvious stronger guided peaks along the vertical (y) direction [see Fig. 6(d)] are unfortunately due to the non-perfect azimuthal structure of the probe vortex beam [see Fig. 6(c)].

Further, we studied the transformation and self-focusing of the azimuthon with five lobes and a central charge-two OV. This structure was generated by another CGH of an OV with TC = 1 and a grating period of 20 μm [Fig. 2(b); see the specific azimuthal modulations, which lead to a decay of the bright ring into five sub-peaks] but this time in the second diffraction order. In this case, the main problem, except for the low efficiency in the second (and each even) diffraction order of the binary hologram, was the slight overlapping of the single peaks. This is due to the fact that the phase jump between each two neighboring peaks was less than π ((4/5)π according to our estimation). The experimental data and the recorded frames for this case can be seen in Fig. 7.

One can see once again the domination of the self-focusing along the nonlinear crystal’s c axis [Fig. 7(b)] and the stronger self-focusing of the peaks along this direction. As in the previous case, the probe beam profile is Laguerre–Gaussian, but this time the vortex is carrying a TC = 1. As a result, as needed, the input bright vortex ring has a smaller diameter. As seen in Fig. 7(d), all waveguides induced are clearly visible and well-formed when illuminated by the infrared probe beam. The different power density distributions of the probe beams in some of the induced waveguides are, unfortunately, again due to the azimuthal irregularity of the probe OV beam’s intensity profile.

The last case that we will discuss here is the self-focusing of a necklace beam with four sub-peaks generated by reproducing a CGH of a quasi-2D dark beam with π phase jumps between each quadrant [see Fig. 2(a)]. After optically inscribing four waveguides in the SBN crystal, the guiding properties of the structure were examined by probe beams with two different (Gaussian and Laguerre–Gaussian) profiles. The experimental results are summarized in Fig. 8. In this case, in addition to the ring-shaped probe beam carrying an OV, we show, for comparison, waveguiding with a Gaussian probe beam. As mentioned, the infrared beam (λ = 808 nm) was emitted by the Ti:Al₂O₃ laser. This time the laser oscillator was mode-locked and emitted sub-30-fs pulses at a repetition rate of some 80 MHz. The aim of this measurement was to show that femtosecond lasers pulses can propagate in the induced waveguides for several minutes without erasing them, provided they are emitted at a wavelength for which the photorefractive crystal has weak photosensitivity. The Gaussian femtosecond probe beam illuminating the induced waveguides is shown in Fig. 8(c). In the lower row of Fig. 8(c), we slightly tilted the experimental frame in order to obtain better visibility of the probe beam on the exit facet of the crystal. As seen, the portions of the guided probe beam appear as four peaks with nearly the same intensities located in the wings of the Gaussian beam. In this case, the central peak of the input Gaussian probe wave remains nearly unaffected by the guiding and is strongly dominating over the guided peaks. This was why we preferred to use vortex rings of different radii (i.e., Laguerre–Gaussian beams) for the measurements presented in Figs. 5 and 6. In the present case of a four-peaked input necklace structure, we also show such data-inscribed waveguides [Fig. 8(b)] illuminated by a vortex probe beam generated from a CGH of an OV with TC = 1 [Fig. 8(d)]. As in the previous two experimental cases reported here, we see a clear waveguiding effect, unfortunately with different exit peak powers of the guided probe beams due to an unwanted irregularity of the vortex ring’s intensity profile on the entrance of the crystal.
Using probe beams, we also examined the time stability of the inscribed waveguiding structures in the SBN crystal with both green probe cw emission (532 nm) and femtosecond laser pulses (at the spectrum central wavelength of 808 nm). The results from these measurements are summarized in the graph shown in Fig. 9. We studied experimentally three cases. In the first case, we illuminated the crystal by the green Gaussian cw laser beam (532 nm), with no electric field biasing the crystal. As one can expect, because the SBN crystals are highly photosensitive in the green spectral range, the beam, which initially induced the waveguides, is now erasing them. In the second case, we illuminated the crystal for a few seconds after large time intervals (blue triangles/line) and by a near-infrared laser beam operated in the same periodic manner (red squares/line).

![Fig. 9](image)

4. CONCLUSION

The experimental data presented show that periodical azimuthal modulation in the reflecting/transmitting stripes of binary computer-generated holograms can lead to a controllable vortex decay into azimuthon beams with an adjustable number of out-of-phase bright lobes. The nonlinearly accelerated defocusing of the central vortex is able to contribute to the initiation of a controllable self-focusing of the bright sub-beams. The results obtained indicate that parallel all-optical guiding of optical signals at wavelengths, for which the medium (a photorefractive crystal) is not photosensitive, is feasible in azimuthon lobes and necklace peaks.

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